

Surfing on a stiffness gradient in skull morphogenesis



Yiteng Dang^{1,2,3}, Adrian A. Lahola-Chomiak¹, Johanna Lattner¹, Diana Alves Afonso¹, Steffen Rulands^{2,3}, Jacqueline Tabler¹

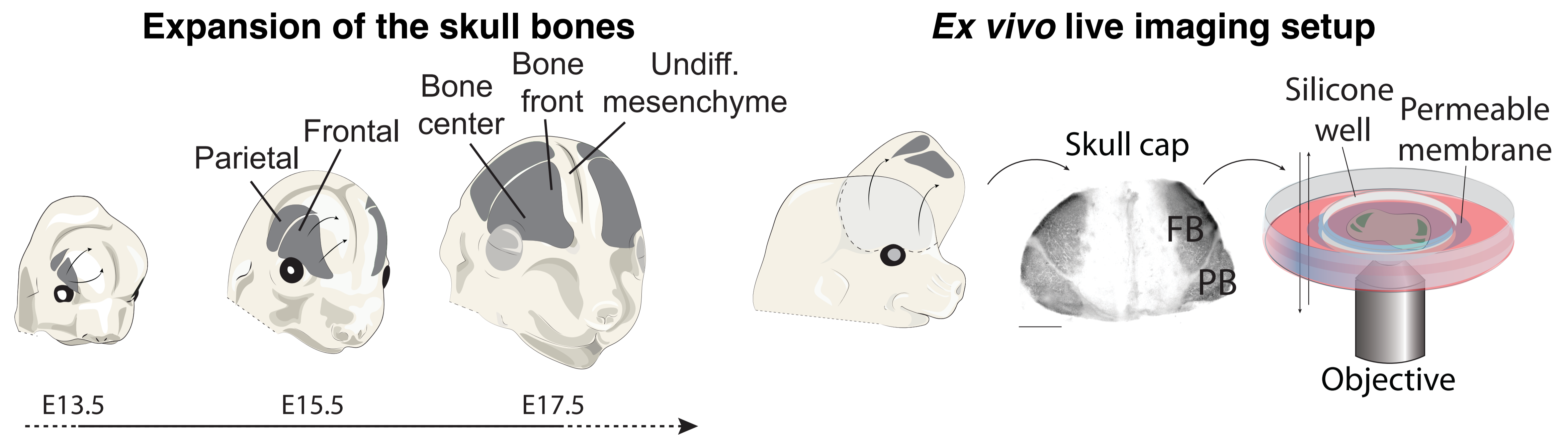
¹Max Planck Institute for Molecular Cell Biology and Genetics, Dresden, Germany

²Max Planck Institute for the Physics of Complex Systems, Dresden, Germany

³Center for Systems Biology, Dresden, Germany

Introduction

During **skull development**, a thin sheet of osteoblasts grows anisotropically from the sides towards the top of the head. How different **cellular behaviours** processes such as proliferation, differentiation and motion collectively drive this expansion remains unclear. Here, we combined **quantitative live imaging**, **atomic force microscopy** and **biophysical modelling** to dissect the different processes driving expansion of a **mesenchymal tissue** in a heterogeneous extracellular environment characterised by a **stiffness gradient**.

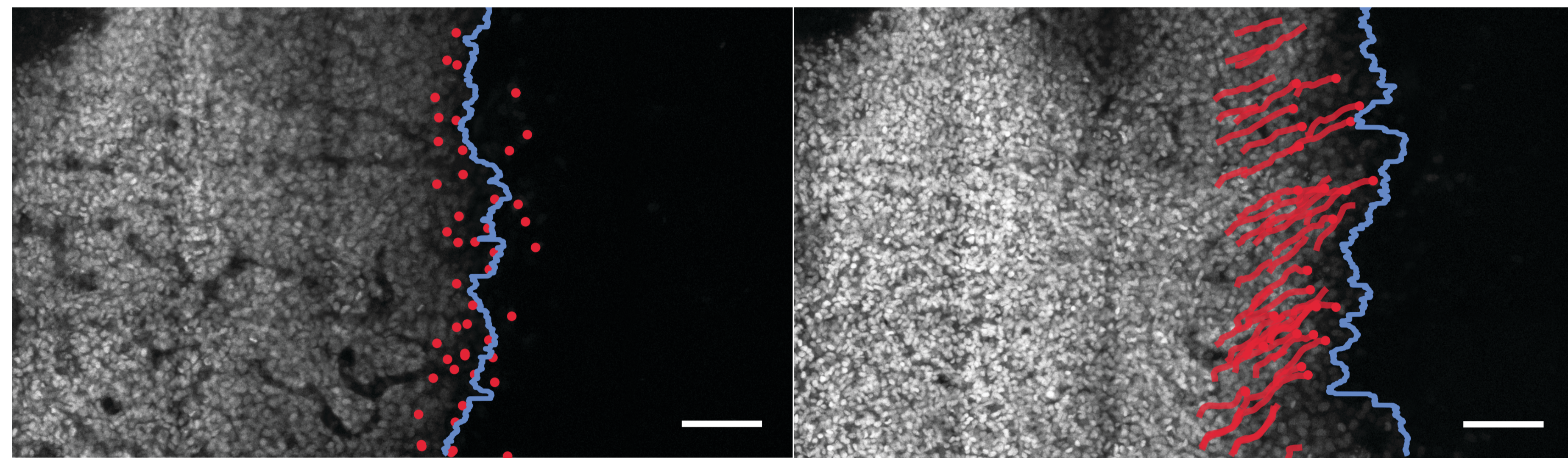


1 Ex vivo live imaging of skull bone expansion

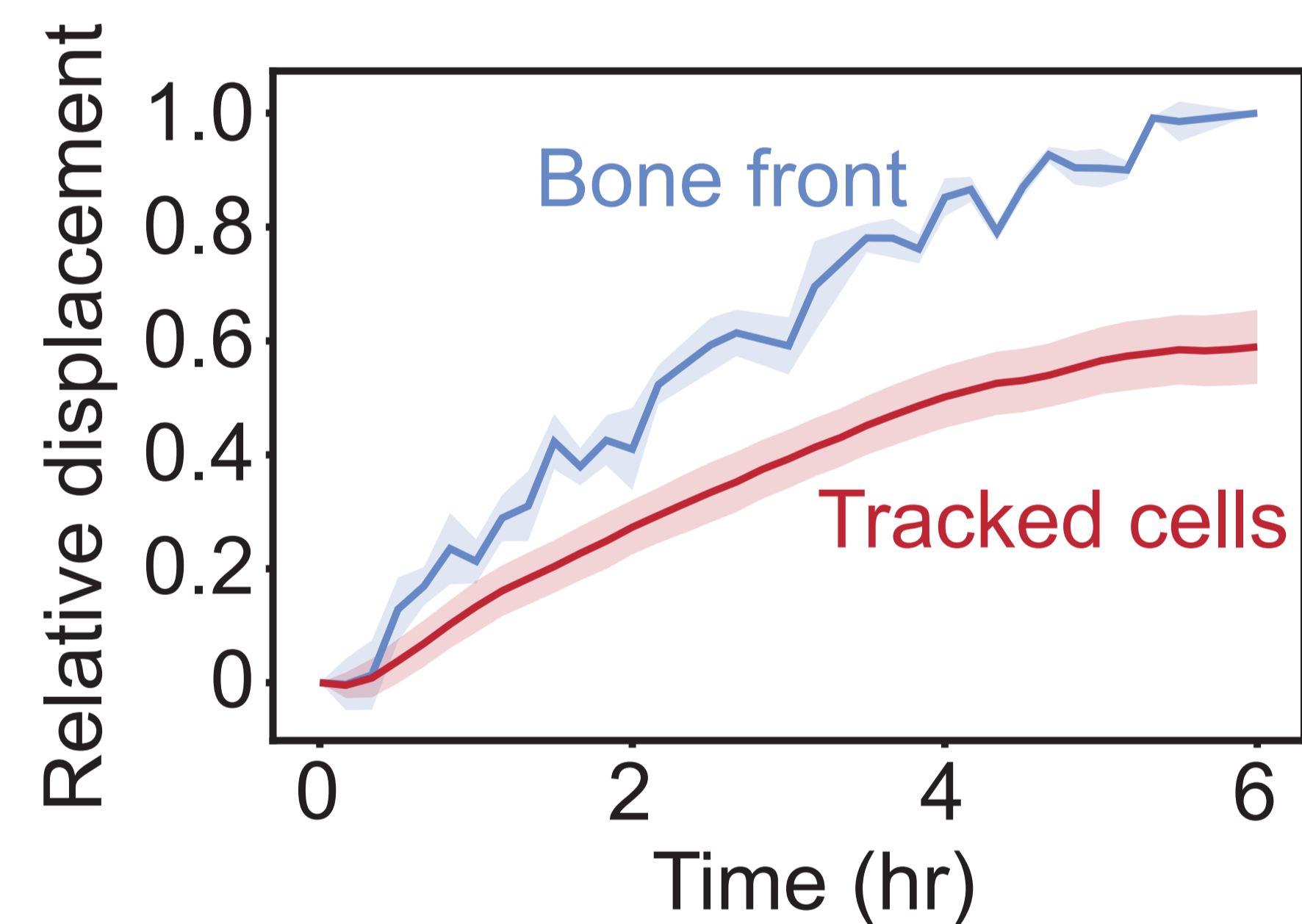
Tracking the bone front and individual osteoblast cells during skull expansion (E13.75)

t = 0 hr

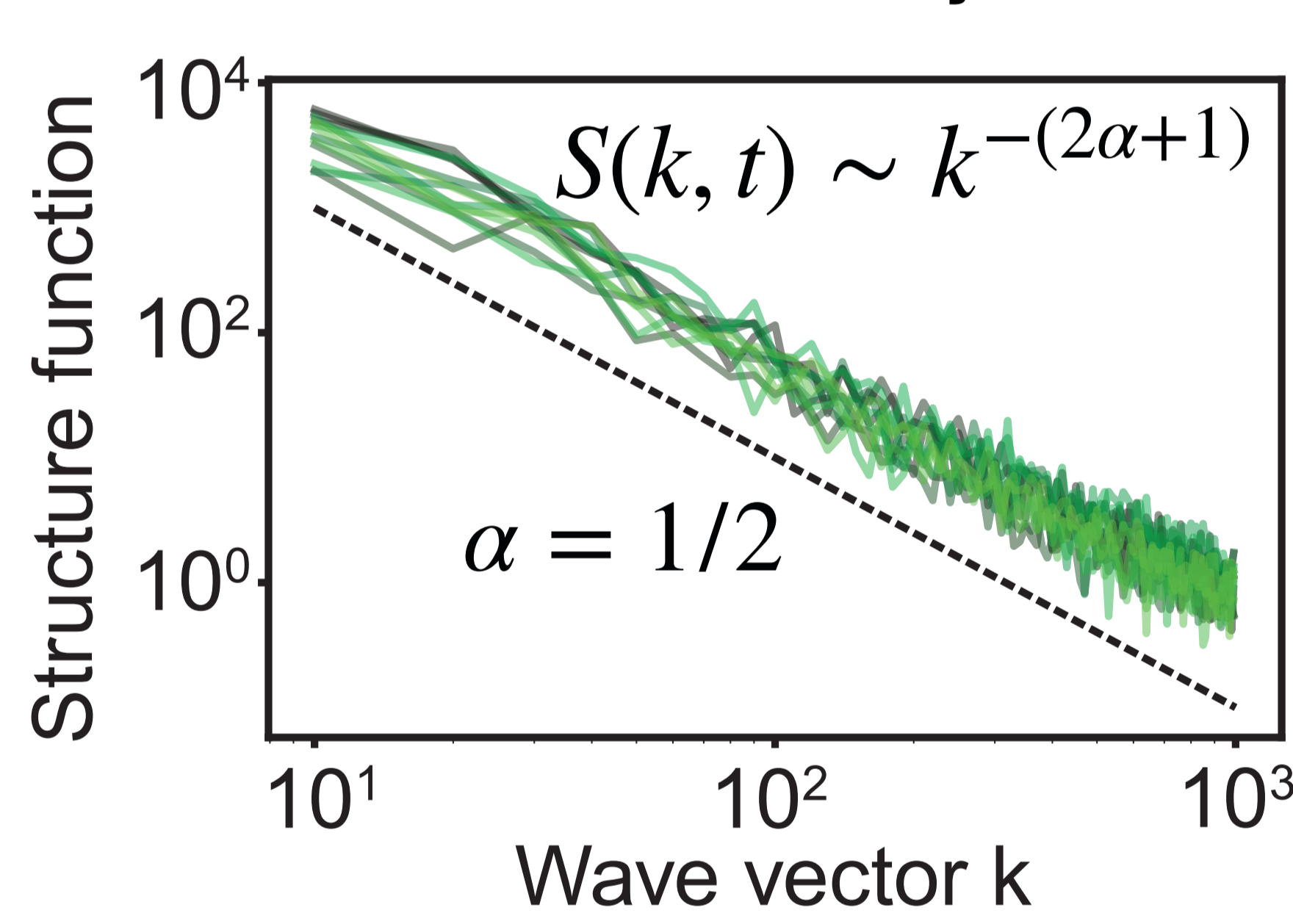
t = 6 hr



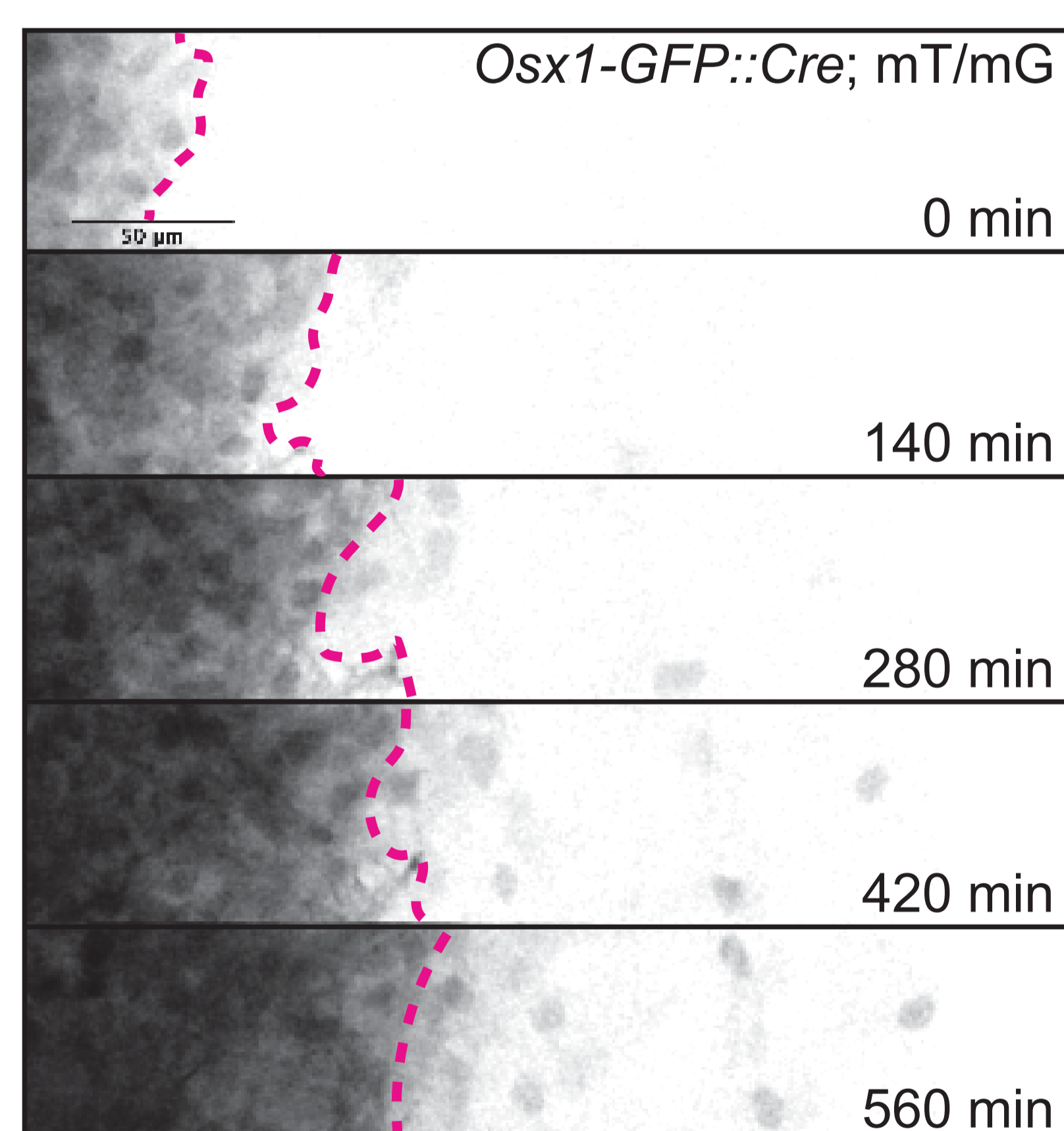
Bone front expands faster than individual cells



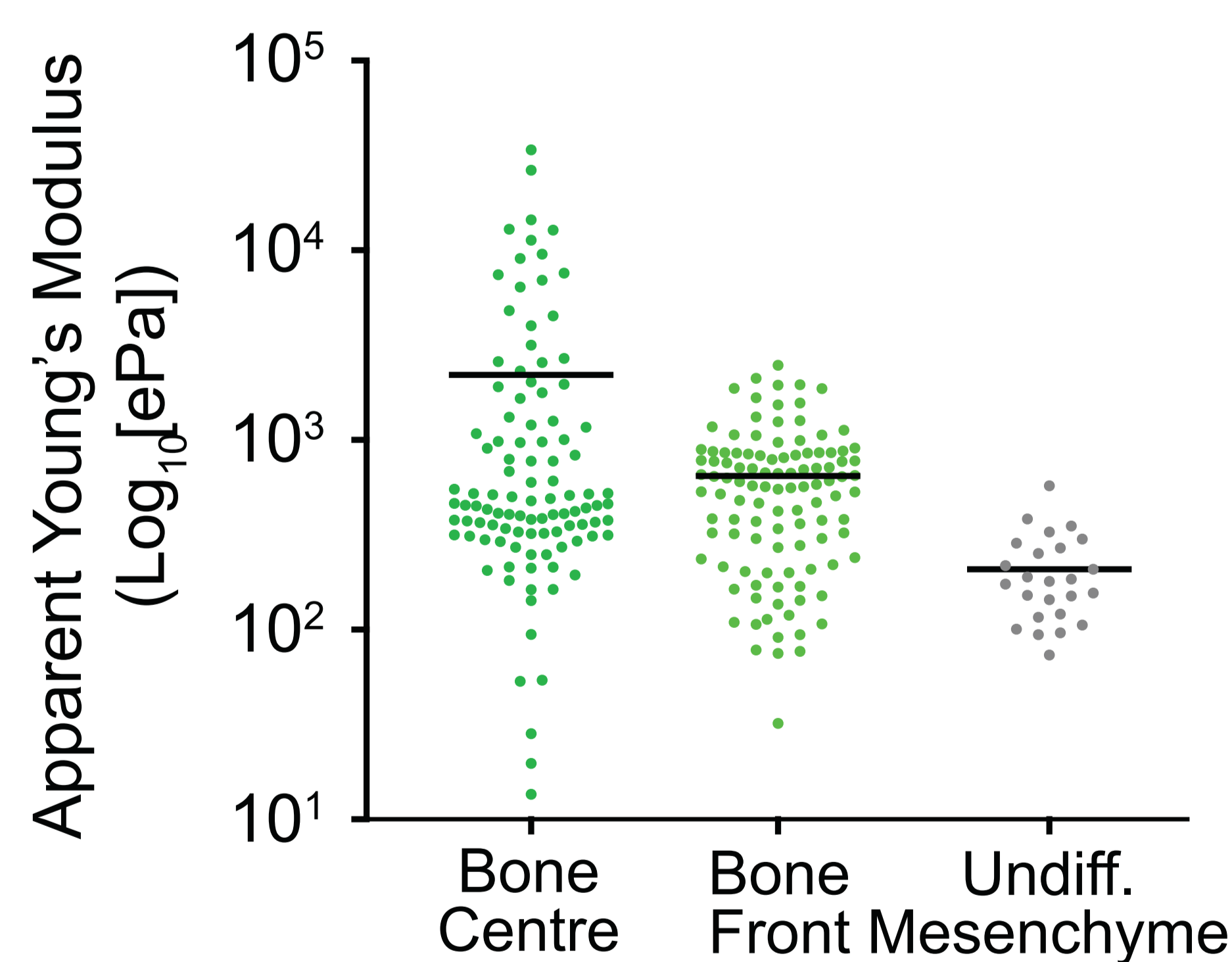
Front roughness is consistent with Fisher-KPP wave dynamics



Differentiation into osteoblasts takes place both at and ahead of the front

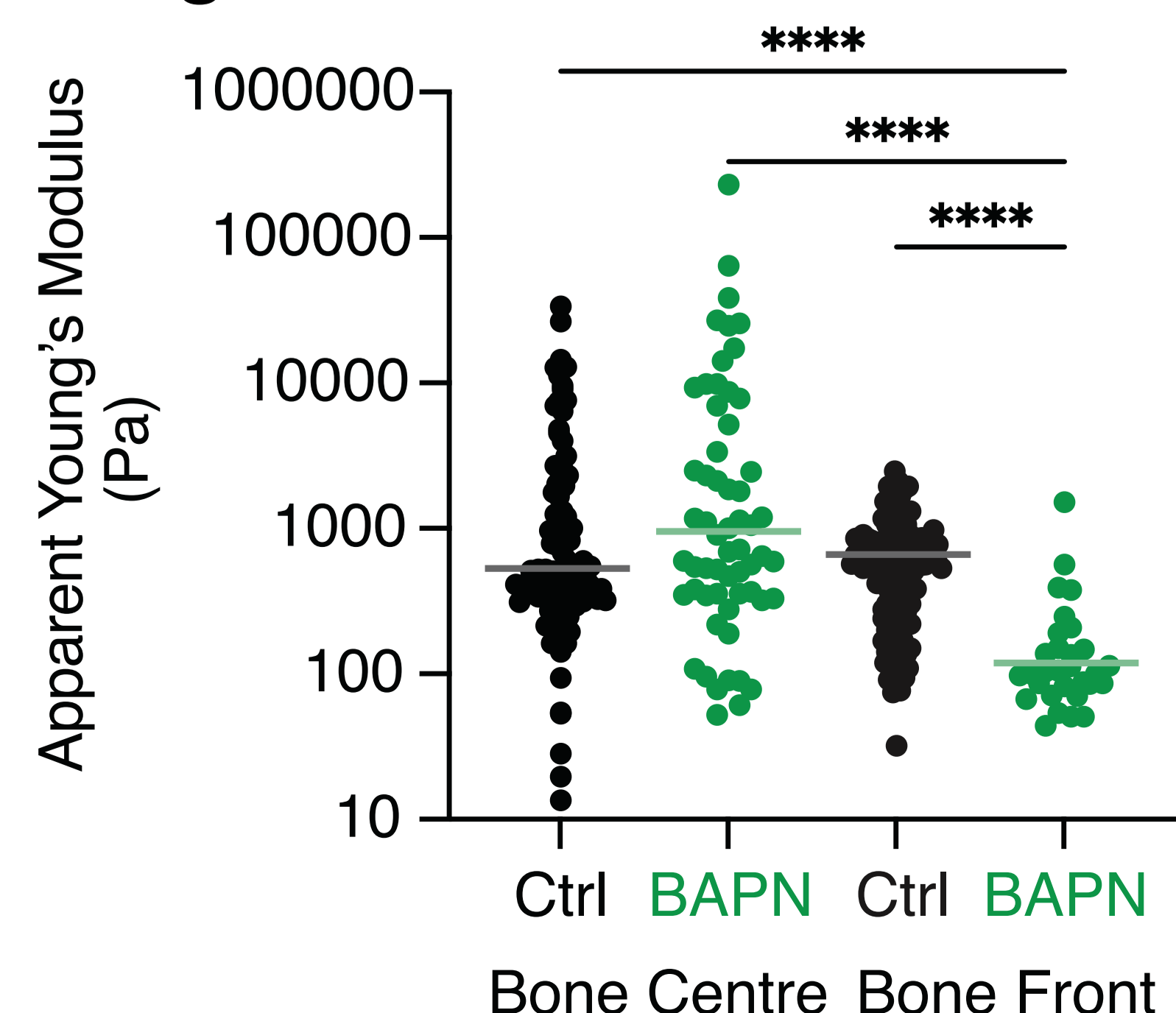


AFM measurements show stiffness gradient along the direction of bone growth

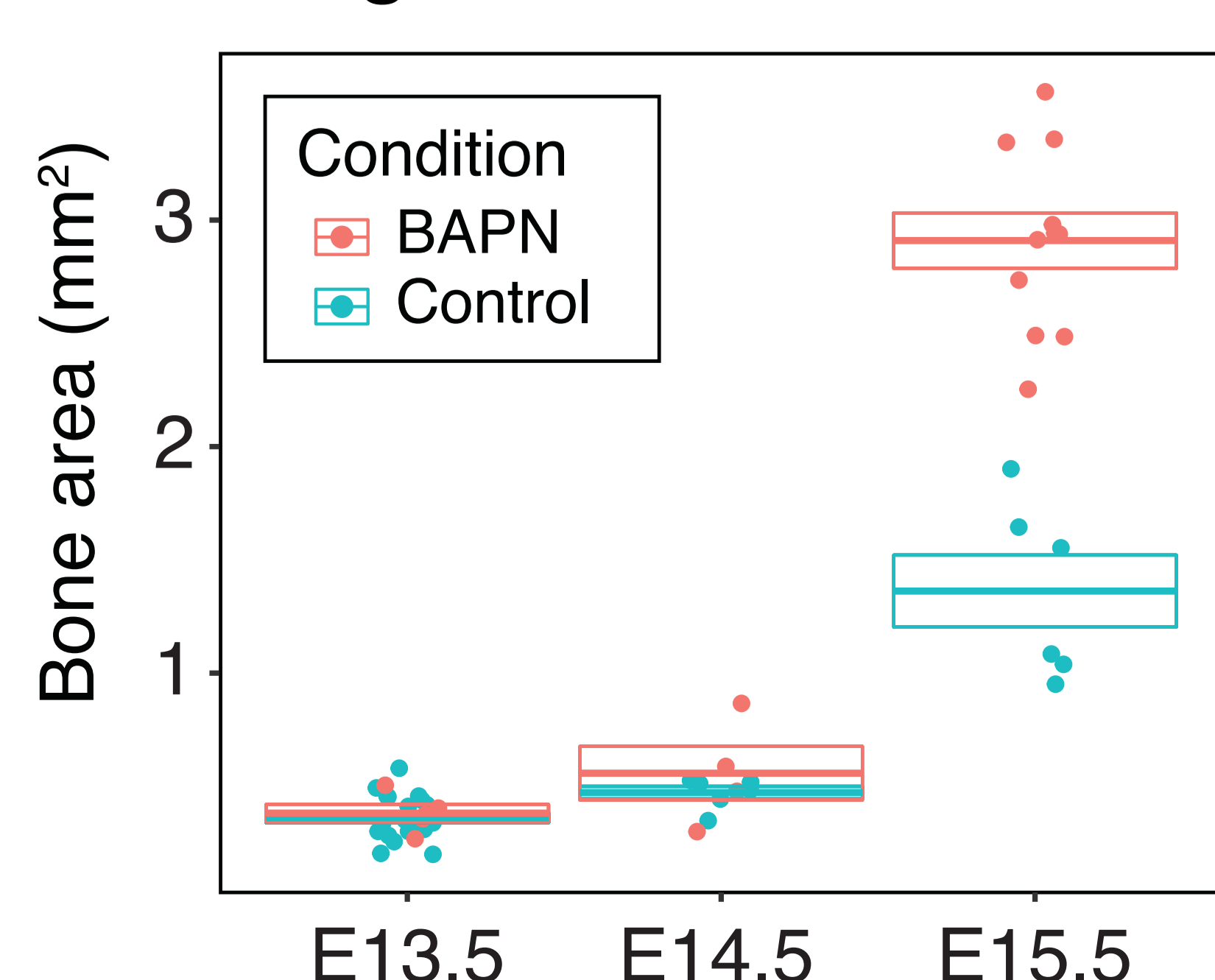


4 BAPN increases stiffness gradient and enlarges bone

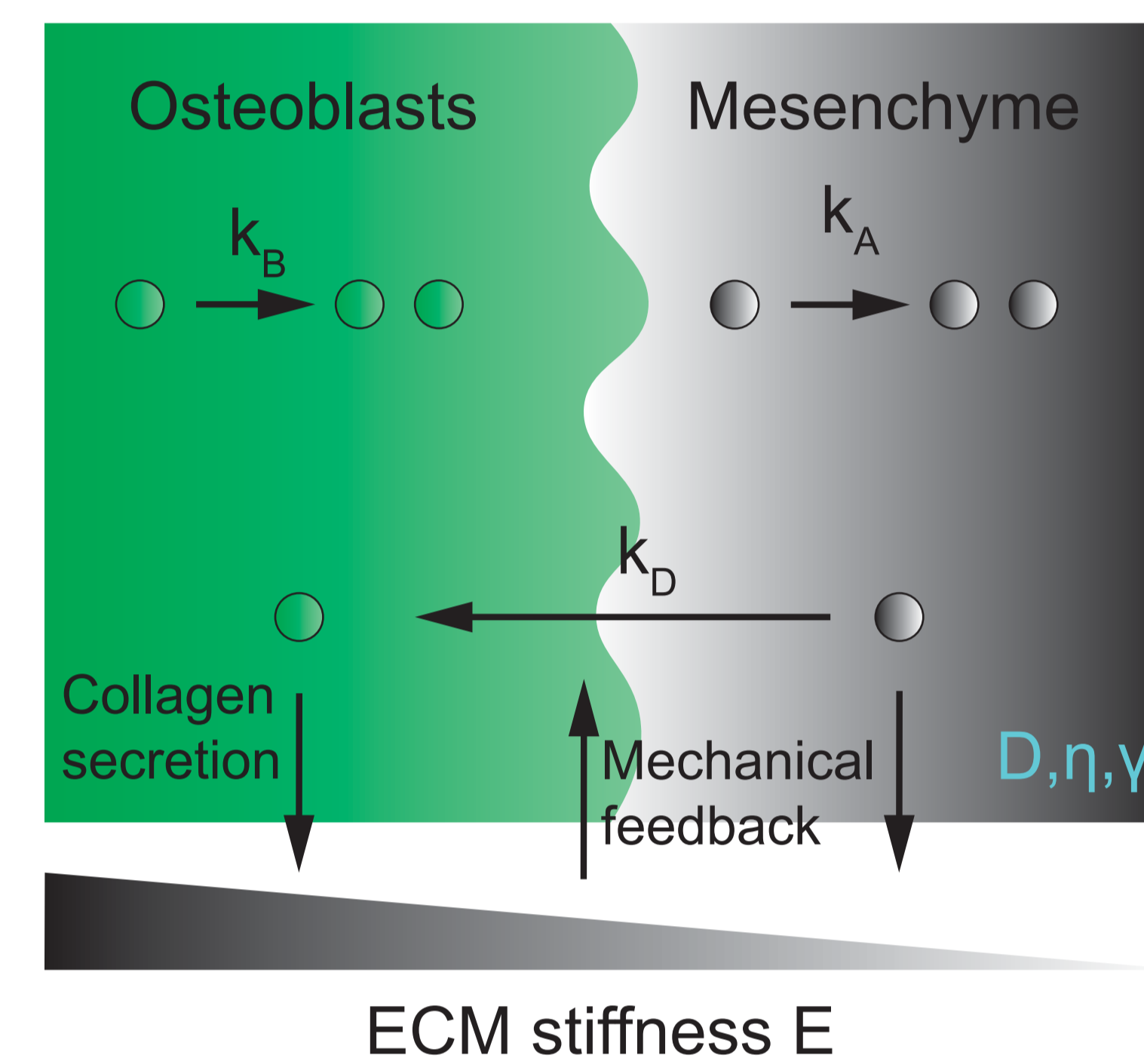
BAPN-treated samples have greater stiffness differential



BAPN-treated samples grow larger bones over time



2 Biophysical model for bone expansion



$$E[\phi] = (E_A + (E_B - E_A)\phi)$$

Differentiation

$$k_D = k_D(E)$$

Fisher-KPP wave dynamics implies $\left. \frac{dk_D}{dE} \right|_{E=E_A} > 0$, to first order $k_D(E) = \alpha(E[\phi] - E_A)$.

Cell number balance

ρ : Total cell density

$$\partial_t \rho + \nabla \cdot (\rho \mathbf{v}) = (k_A(1 - \phi) + k_B \phi) \rho$$

Advection Cell division/death

Differentiation dynamics

ϕ : Fraction of osteoblasts

$$\partial_t \phi + \mathbf{v} \cdot \nabla \phi = D \frac{1}{\rho} \nabla \cdot (\rho \nabla \phi) + (k_B - k_A) \phi(1 - \phi) + k_D(1 - \phi)$$

Advection Diffusion Proliferation gradient Differentiation

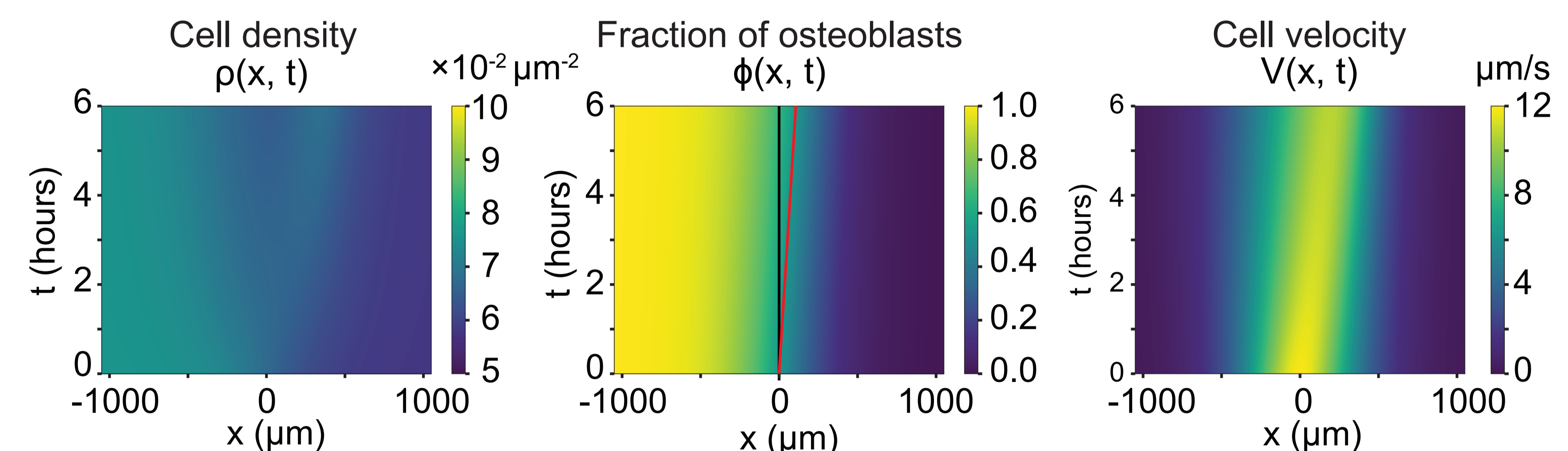
Force balance

\mathbf{v} : Advection velocity

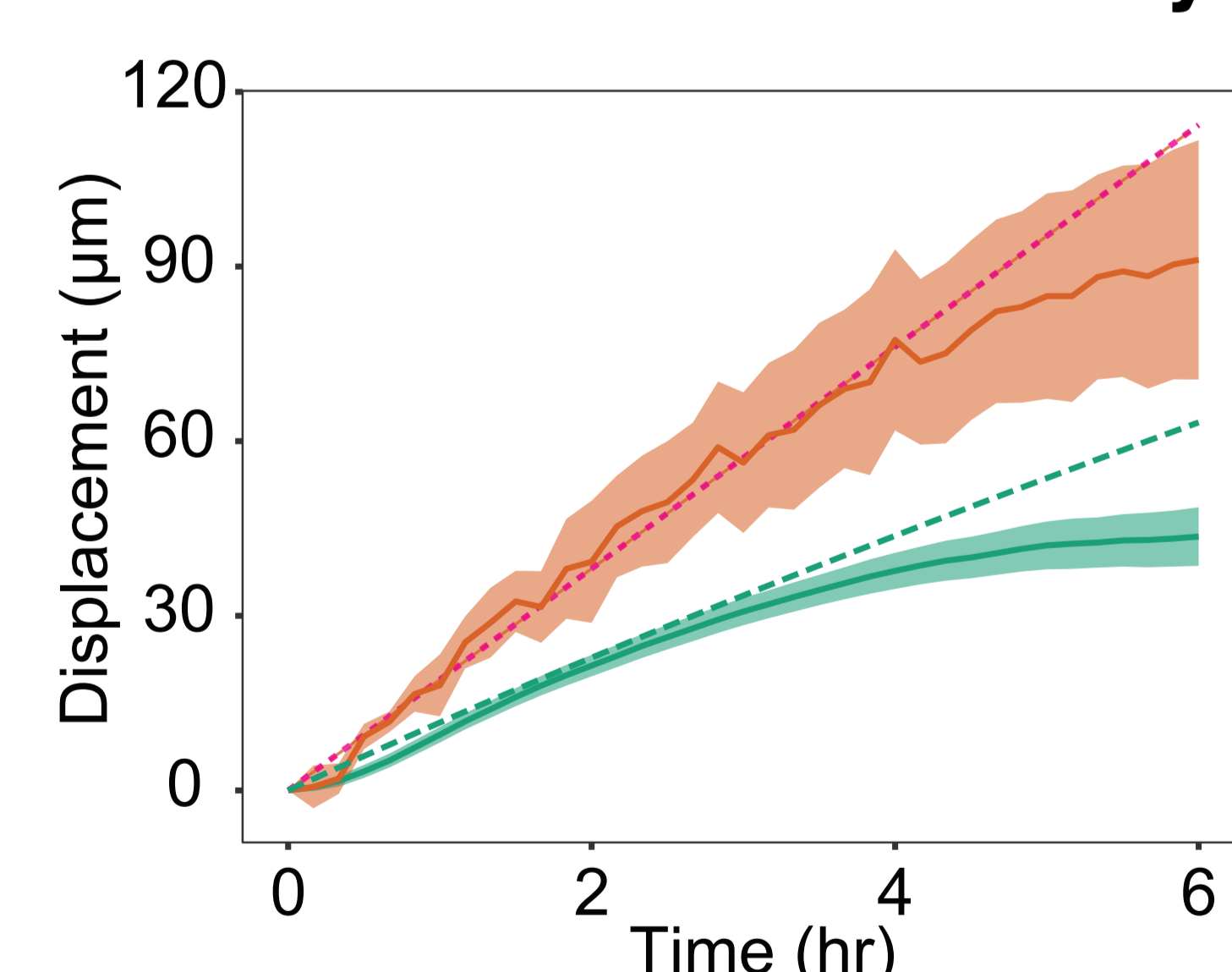
$$\nabla \cdot \sigma = \gamma \mathbf{v} \quad \sigma = -P\mathbf{I} + 2\tilde{\eta}\tilde{\mathbf{v}} + \xi(\nabla \cdot \mathbf{v})\mathbf{I}$$

Friction Constitutive equation for a viscous fluid

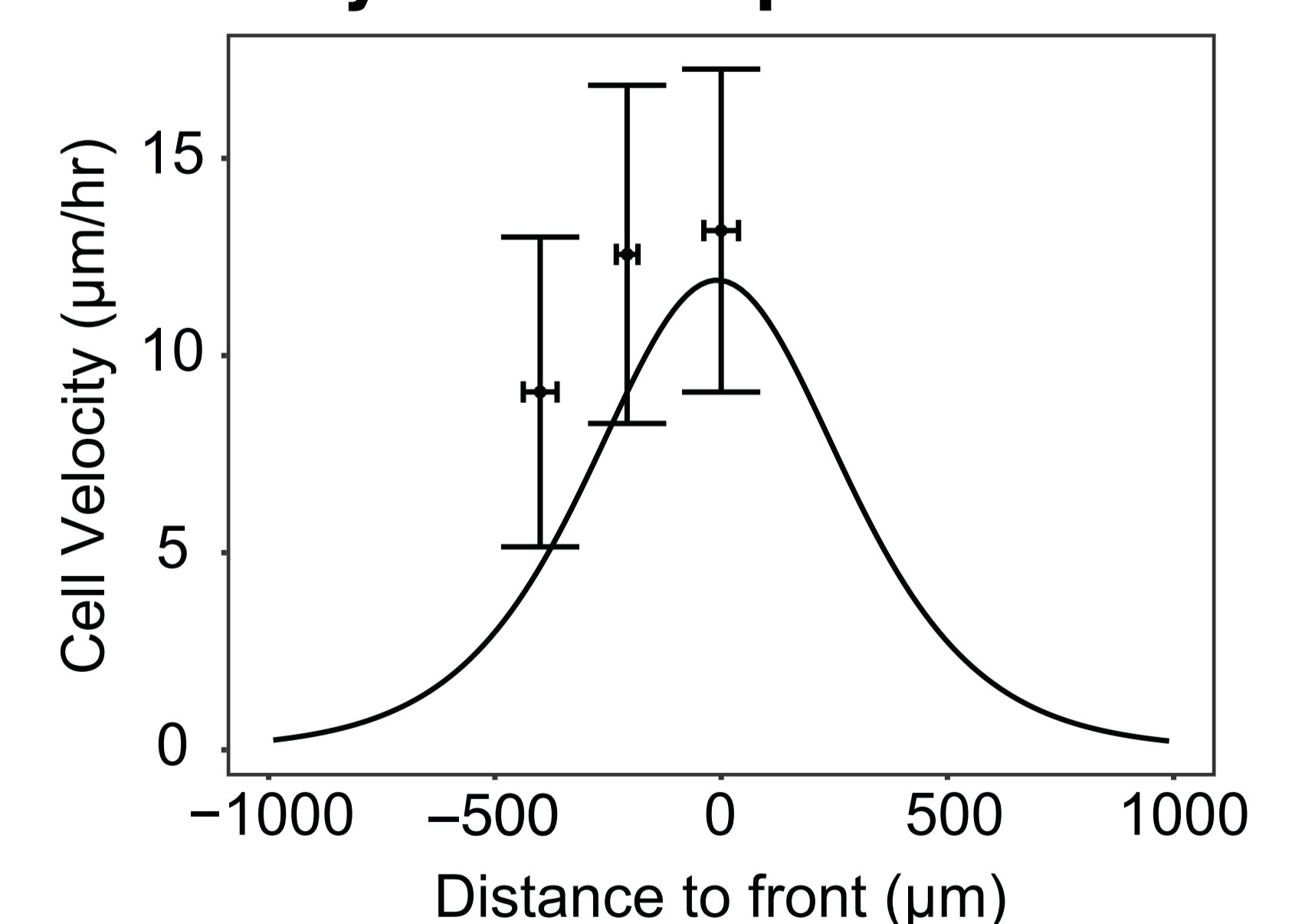
3 Biophysical model recapitulates experimental results



Model fits cell and front dynamics



Cell velocity shows a peak at the front



Conclusion

- Skull development reveals biophysical mechanisms controlling **mesenchymal morphogenesis**.
- Mechanical feedback** orchestrates cell differentiation *and* cell motion.
- Mathematical modelling** reveals simplicity that underscores robustness of morphogenesis.

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